

# High performance characteristics of dual pumped $\text{Er}^{+3}/\text{Yb}^{3+}$ Co-doped/Raman hybrid optical amplifier

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In this paper, a hybrid optical amplifier is suggested comprising an  $\text{Er}^{3+}/\text{Yb}^{3+}$  co-doped fiber amplifier (EYCDFA) as a pre-amplifier and a Raman fiber amplifier (RA) as a post amplifier. The performance characteristics of the hybrid amplifier (EYCDRHA) are theoretically and experimentally studied including gain and noise figure. In the theoretical model, the amplified spontaneous emission (ASE) as well as the background losses and the up-conversion effect between  $\text{Er}^{3+}$  ions and  $\text{Yb}^{3+}$  ions are taken into consideration. The performance characteristics are investigated using dual pump configuration, forward EYCDFA pump at 980 nm and backward RA pump at 1450 nm at different values of input signal power, EYCDFA and RA pump powers and lengths at two different values of input signal wavelength; 1530 and 1600 nm. A high gain and low noise performance are obtained for the suggested amplifier. Furthermore, a good agreement between the theoretical and experimental values of the gain and noise figure at the input parameters is obtained.

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## 1. Introduction

The phosphate as host glass has an important feature when doped by Er/Yb to form a co-doped fiber amplifier (EYCDFA). It offers a low cooperative up-conversion coefficient of the  $^4I_{13/2}$  level of the  $\text{Er}^{3+}$  ions [1-3]. Many candidates reported the performance of highly Er/Yb co-doped multimode phosphate glass fibers which were used in high gain short-length amplifiers [4-6]. In Ref. [7], a single-mode highly Er/Yb co-doped phosphate glass-fiber is fabricated by rod-in tube technique. Its gain and noise figure are measured by dual-pump configuration at -30, -10 and -1 dBm input signal level. A net gain coefficient is obtained as high as 3.3 dB/cm from a micro erbium doped fiber amplifier (EDFA) based on a 5 cm long phosphate fiber. Furthermore, when  $\text{Yb}^{3+}$  ion is doped with  $\text{Er}^{3+}$  ion in the host glass, it provides several advantages including stronger absorption band in the region 880-1050 nm and a large overlap between  $\text{Yb}^{3+}$  emission and  $\text{Er}^{3+}$  absorption which makes the EYCDFA suitable to obtain large gain [8].

The use of distributed Raman amplification in fibers can provide improved noise figure, signal power gain and optical signal to noise ratio (OSNR) [9]. The hybrid amplifier is a combination of two amplifiers for obtaining higher gain and lower noise figure than the single amplifier. EDFA/Raman with hybrid configuration has been extensively studied showing low noise figure and high gain for transmission systems compared to conventional EDFA [10-12]. Simranjit Singh and R.S. Kaler provided an analytical model of EDFA-Raman hybrid optical amplifier and optimized the various parameters using genetic algorithm method [13].

Furthermore, the L-band remote EDFA/Raman hybrid amplifier was experimentally investigated for flat gain [14].

In this paper, the performance characteristics of EYCDFA/Raman hybrid amplifier (**EYCDRHA**) are investigated experimentally and theoretically. A hybrid amplifier comprises a two-stage erbium-ytterbium co-doped fiber amplifier of length (0.5-1.2 m) at forward 980 nm pump of power (100- 500 mW) as pre-amplifier and Raman fiber amplifier of length (10- 45 km) at backward 1450 nm pump of power (50-250 mW) as a post amplifier. The input signal power varies from - 40 to 10 dBm at two different values of signal wavelength; 1530 and 1600 nm, which are the start and end points of the signal wavelength range. The proposed theoretical model takes into account the amplified spontaneous emission (ASE), the background losses and the up-conversion effect of EYCDFA.

## 2. Basic model

First, we consider the rate and power equations of the signal, pump and ASE in the pre-amplifier (EYCDFA), where the input signal power in EYCDFA is  $P_{s1}(0)$  and the output signal power is  $P_{s1}(L_{\text{EYDFA}})$ . Second, we consider the power equations in the post amplifier (RA), where the input signal power is  $P_{s2}(0) = P_{s1}(L_{\text{EYDFA}})$  and the output signal power is  $P_{s2}(L_{\text{RA}})$ , where  $L_{\text{EYDFA}}$  is the EYCDFA length and  $L_{\text{RA}}$  is the RA length. Fig. 1 represents the energy level diagram of the  $\text{Er}^{3+}/\text{Yb}^{3+}$  system.

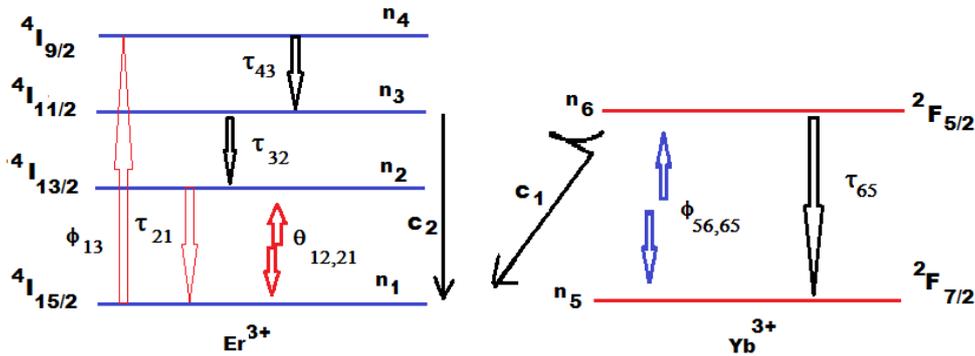


Fig. 1. The energy level diagram for  $Er^{3+}/Yb^{3+}$  co-doped system.

The theoretical model depends on the energy level diagram of EYCDF in Fig. 1. Neglecting the spontaneous emission life time between levels 4 and 3,  $\tau_{43}$  and the number of Er ions in level 4,  $n_4$ , and using Ref. [15], one can get the rate equations of Er/Yb co-doped fiber amplifier as

$$\frac{dn_1}{dt} = \frac{n_2}{\tau_{21}} - \theta_{12}n_1 + \theta_{21}n_2 - \phi_{13}n_1 + C_2n_2^2 + C_2n_3^2 - C_1n_1n_6 \quad (1)$$

$$\frac{dn_2}{dt} = \frac{n_3}{\tau_{32}} - \frac{n_2}{\tau_{21}} - \theta_{21}n_2 + \theta_{12}n_1 - 2C_2n_2^2 \quad (2)$$

$$\frac{dn_3}{dt} = -\frac{n_3}{\tau_{32}} + \phi_{13}n_1 - 2C_2n_3^2 + -C_1n_3n_5 + C_1n_1n_6 \quad (3)$$

$$\frac{dn_6}{dt} = -\frac{n_6}{\tau_{65}} + \phi_{56}n_5 - \phi_{65}n_6 + C_1n_3n_5 - C_1n_1n_6 \quad (4)$$

$$n_1 + n_2 + n_3 = n_{Er} \quad (5)$$

$$n_5 + n_6 = n_{Yb} \quad (6)$$

Here,  $\tau_{ij}$  refers to the spontaneous emission lifetimes between levels  $i$  and  $j$ ,  $\theta_{12}$  and  $\theta_{21}$  are, respectively, the signal absorption and emission rates of  $Er^{3+}$ ,  $\Phi_{13}$  is the pump absorption rate of  $Er^{3+}$  and  $\Phi_{56}$  and  $\Phi_{65}$  are the pump absorption and emission rates of  $Yb^{3+}$ , respectively.  $C_1$  and  $C_2$  are the cross-relaxation and up-conversion coefficients,

$$\frac{dP_{s1}(z)}{dz} = [\Gamma_{s1}(v_{s1})\{\sigma_{21}(v_{s1})n_2(z) - \sigma_{12}(v_{s1})n_1(z)\} - \alpha_{s1}(v_{s1})]P_{s1}(z) \quad (9)$$

$$\frac{dP_{p1}(z)}{dz} = [\Gamma_{p1}(v_{p1})\{\sigma_{65}(v_{p1})n_6(z) - \sigma_{56}(v_{p1})n_5(z) - \sigma_{13}(v_{p1})n_1(z)\} - \alpha_{p1}(v_{p1})]P_{p1}(z) \quad (10)$$

$$\frac{dP_{ASE}^{\pm}(z)}{dz} = \pm hv_{p1}\Delta v\Gamma_{p1}(v_{p1})\sigma_{65}(v_{p1})n_6(z) \cdot [\Gamma_{p1}(v_{p1})\cdot\{\sigma_{65}(v_{p1})n_6(z) - \sigma_{56}(v_{p1})n_5(z)\} - \alpha(v)]P_{ASE}^{\pm}(z) \quad (11)$$

where  $\alpha(v_{s1})$ ,  $\alpha(v_{p1})$  and  $\alpha(v)$  are the frequency-dependent background losses at the signal, pump and ASE bandwidth,  $\Gamma_s$  and  $\Gamma_p$  are the overlapping factors of the light signal and pump light, respectively.  $\sigma_{12}(v_s)$ ,  $\sigma_{21}(v_s)$  and  $\sigma_{13}(v_p)$  are the emission/absorption cross-sections at the optical frequency  $v$  for the  $Er^{3+}$  while  $\sigma_{54}(v_p)$  and  $\sigma_{45}(v_p)$  are the emission and absorption cross-sections for the  $Yb^{3+}$ .

The output signal from the pre-amplifier and noise figure are, respectively, given by [15-18]

respectively.  $C_2n_2^2$  and  $C_2n_3^2$  are terms accounting for uniform up-conversion, and  $C_1n_3n_5$  and  $C_1n_1n_6$  are terms representing the energy transfer between  $Er^{3+}$  to  $Yb^{3+}$  and  $Yb^{3+}$  to  $Er^{3+}$ , respectively.

The transition rates  $\phi_{ij}$ ,  $\theta_{ij}$  are given by [15]

$$\phi_{ij}, \theta_{ij} = \frac{\sigma_{ij}(v_{p,s})}{hv_{p,s}} P_{p,s}(z) |E(r, v_{p,s})|^2 + \int_0^{\infty} \frac{\sigma_{ij}(v_{p,s})}{hv_{p,s}} [P_{ASE}^+ + P_{ASE}^-] \cdot |E(r, v_{p,s})|^2 dv \quad (7)$$

where  $\sigma_{ij}$  is the cross-section of signal and pump,  $v_s$  and  $v_p$  are the signal and pump frequencies, respectively,  $h$  is the Planck's constant,  $P_s$  and  $P_p$  are the signal and pump powers, respectively,  $P_{ASE}^{\pm}(z, v)$  are the forward (plus sign) and backward (minus sign) ASE powers, respectively, at a frequency  $v$  in a frequency interval  $\Delta v$  and at the longitudinal fiber coordinate  $z$ .  $E(v, r)$  is the field distribution of the  $LP_{01}$  mode.

The value of  $E(v, r)$  can be obtained through normalization as [16]

$$2\pi \int_0^{\infty} |E(r, v_{p,s})|^2 r dr = 1 \quad (8)$$

The power propagation equations along the EYDF for signal, pump and ASE are given as [16]

$$P_{s1}(L_{EYDFA}) = G_{EYDFA} P_{s1}(0) \quad (12)$$

$$NF_{EYDFA} = \frac{1}{G_{EYDFA}} + \frac{P_{ASE}^{\pm}(v, z)}{G_{EYDFA} h v_s \Delta v_s} \quad (13)$$

where  $G_{EYDFA}$  is the gain of the pre-amplifier (EYCDFA).

For Raman amplifier, the rate equation can be written as [19]

$$\frac{dP_{s2}(z)}{dz} = -\alpha_{sR} P_{s1} + \frac{g_{RP} P_p P_{s1}}{\gamma_p} \quad (14)$$

$$-\frac{dP_{pR}}{dz} = -\alpha_{pR}P_{pR} + \frac{f_{pR}g_R P_{pR}P_{s1}}{f_{sR}\gamma_p} \quad (15)$$

where  $P_{s2}$  is input signal power for Raman amplifier, which is the also the output signal power of EYCDFA,  $g_R$  is Raman gain coefficient,  $P_{pR}$  is the pump power for Raman amplifier,  $\gamma_p$  is the cross-sectional area of pump beam inside the fiber,  $\alpha_{sR}$  and  $\alpha_{pR}$  is fiber losses at signal and pump at frequencies  $f_{sR}$  and  $f_{pR}$ . The negative sign indicates the backward pumping.

The Raman gain coefficient is calculated from the relation [20]

$$g_R = \gamma_s(\nu) \frac{\lambda_s^3}{c^2 h(n(\nu))^2} \quad (16)$$

$\gamma_s$  is the Raman cross section of the signal,  $\lambda_s$  is the Stokes wavelength and  $n(\nu)$  is the frequency dependent refractive index.

The gain of Raman amplifier is given as

$$G_{Raman} = 10 \log_{10} \left\{ \frac{P_{s2}(L_{Raman})}{P_{s1}(L_{EYDFA})} \right\} \quad (17)$$

Now, the noise figure of Raman can written as [19]

$$NF_{Raman} = \frac{2(P_{ASE}^-)_{Raman}}{h\nu_{sr}\Delta\nu_r G_{Raman}} + \frac{1}{G_{Raman}} \quad (18)$$

where  $\Delta\nu_r$  is the reference optical bandwidth corresponding to 0.1 nm [21, 22].

The gain of EYCDFA/Raman hybrid amplifier (EYCDRHA),  $G_{HA}$ , is given by [20]

$$G_{HA} = 10 \log_{10} \left( \frac{P_{s2}(L_{Raman})}{P_{s1}(0)} \right) \quad (19)$$

and the net noise figure for the EYCDRHA is [19]

$$NF_{HA} = \frac{1}{G_{EYDFA}} + \frac{P_{ASE}^+(v,z)}{G_{EYDFA}h\nu_s\Delta\nu_s} + \frac{NF_{Raman}-1}{G_{EYDFA}} \quad (20)$$

### 3. Numerical analysis

The results of theoretical model are obtained by solving Eqs. (9)-(11) for the EYCDFA at different values of pump and signal powers. The boundary conditions are taken as  $P_{p1}(z=0) = P_{p1} = (100-500 \text{ mW})$ ,  $P_{s1}(0) = P_{s1} = (-40 \text{ to } +10 \text{ dBm})$  and  $P_{ASE}^+(z=0, \nu) = P_{ASE}^-(z=L_{EYDFA}, \nu)$ . The solution of the rate equations Eqs. (1)-(6) is obtained under the condition  $dn_i/dt = 0$  and the numerical solution of the equations is performed using Runge-Kutta iterative procedure. The output signal  $P_{s1}(L_{EYDFA})$  of EYCDFA is considered as input signal  $P_{s2}(0)$  for Raman amplifier.

Equations (14) and (15) are solved using the cross section evaluated in Eq. (16), with boundary conditions  $P_{pR}(z=0) = P_{pR} = (50-250 \text{ mW})$  to obtain the output signal of Raman amplifier  $P_{s2}(L_{Raman})$ . Now, we can find the gain and noise figure of hybrid amplifier using Eqs. (19) and

(20). For each operating wavelength, the absorption and emission of both Er and Yb in the EYD phosphate glass in Ref. [23] are used and the cross section of Raman fiber in Ref. [20, 24] is used in Eq. (16). All input parameters used in the theoretical model for EYCDFA and Raman amplifier are listed in Tables 1-3.

Table 1. EYCDRHA [19-23].

Parameter	Symbol	Value	Unit
Raman pump power	$P_{pR}$	(50-250)	mW
EYDFA pump power	$P_{p1}$	100 – 500	mW
RA length	$L_R$	10-45	km
EYDFA length	$L_{EYDFA}$	0.5 - 1.2	m
Number of input signal channels	$N_{in}$	70	-
Number of output signal channels	$N_{out}$	70	-

Table 2. EYCDFA parameters [15-18].

Parameter	Symbol	Value	Unit
Pump wavelength	$\lambda_p$	980	nm
Signal wavelength	$\lambda_s$	1530	nm
Er concentration	$N_{Er}$	$5.14 \times 10^{25}$	$m^{-3}$
Yb concentration	$N_{Yb}$	$6.2 \times 10^{26}$	$m^{-3}$
Er <sup>3+</sup> absorption cross-section	$\sigma_{13}$	$2.58 \times 10^{-25}$	$m^2$
Yb <sup>3+</sup> absorption cross-section	$\sigma_{45}$	$1.0 \times 10^{-24}$	$m^2$
Yb <sup>3+</sup> emission cross-section	$\sigma_{54}$	$1.0 \times 10^{-24}$	$m^2$
Er <sup>3+</sup> absorption cross-section	$\sigma_{12}$	$6.5 \times 10^{-25}$	$m^2$
Er <sup>3+</sup> emission cross-section	$\sigma_{21}$	$7.0 \times 10^{-25}$	$m^2$
Er <sup>3+</sup> emission lifetime	$\tau_{21}$	10	ms
Yb <sup>3+</sup> emission lifetime	$\tau_{65}$	1.5	ms
Life time	$\tau_{32}$	$10^{-9}$	s
Cross-relaxation coefficient	$C_1$	$3.44 \times 10^{-22}$	$m^3/s$
Up-conversion coefficient	$C_2$	$5.2834 \times 10^{-22}$	$m^3/s$
Core radius	$a$	2	$\mu m$
Doping radius	$r$	2	$\mu m$
Numerical aperture	NA	0.15	-
Core refractive index	$n_1$	1.52812	-
Cladding refractive index	$n_2$	1.51	-
Amplifier cross-section	$A_{eff}$	50	$\mu m^2$
Pump overlap factor	$\Gamma_p$	0.921	-
Signal overlap factor	$\Gamma_s$	0.795	-
Signal loss	$\alpha_{s1}$	0.1	dB/m
Pump loss	$\alpha_{p1}$	0.15	dB/m
Amplified spontaneous emission	$P_{ASE}^+(0)$	0.15	mW

Table 3. RA parameters [19-23].

Parameter	Symbol	Value	Unit
Raman gain coefficient	$g_R$	$10 \times 10^{-14}$	-
Reference optical bandwidth	$\Delta\nu_r$	0.1	nm
Pump wavelength	$\lambda_{pR}$	1450	nm
Fiber loss at signal frequency	$\alpha_{sR}$	$2.3 \times 10^{-5}$	dB/m
Fiber loss at pump frequency	$\alpha_{pR}$	$2.33 \times 10^{-5}$	dB/m
Cross-sectional area of pump beam	$\gamma_s$	$10.2 \times 10^{12}$	$m^2$
Cross-sectional area of signal beam	$\gamma_p$	$11.5 \times 10^{12}$	$m^2$
Amplified spontaneous emission	$P_{ASE}^+(0)$	0.22	mW

#### 4. Experimental setup

Fig. 2 shows the EYCDRHA experimental setup, designed by Optisystem ver.7.1. The system consists of 70 channels covering the wavelength range 1525-1610 nm. This is performed using a continuous wave (CW) laser array. The 980 nm pump laser used for EYCDFA is of 300 mW forward with multiplexed signals through the pump coupler. An erbium-ytterbium doped phosphate glass fiber is chosen at lengths of 0.7-1 m. The output of EYCDFA is directed from the isolator to a Raman phosphate based glass of lengths 25 km. The Raman amplifier is backward pumped with 200 mW at 1450 nm. The output signals are demultiplexed by fiber Bragg gratings and are recorded by the optical receiver.

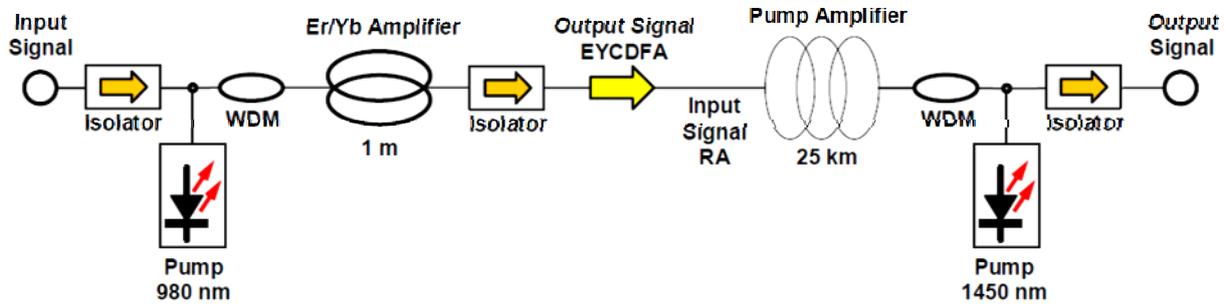


Fig. 2. Hybrid EYCDFA/Raman amplifier setup.

#### 5. Results and discussion

Fig. 3 shows the obtained gain theoretically and experimentally of the EYCDRHA as a function of input signal power at RA length of 25 km and pump power of 200 mW, Er/Yb co-doped amplifier length of 1m and pump power of 500 mW, at two different values of signal wavelengths 1530 and 1600 nm, respectively.

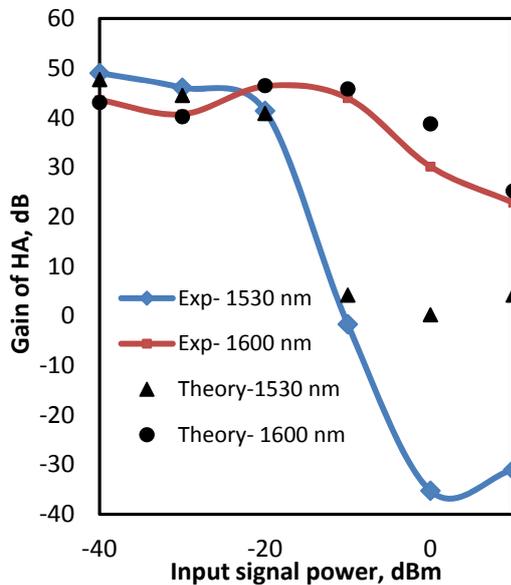


Fig. 3. Gain of HA versus the input signal power.

At 1530 nm, it is clear that, the gain has a maximum value 49 dB at - 40 dBm signal power, and the gain is positive for input signal power < 10 dBm. A good agreement is noticed between the theoretical and experimental results of the gain.

The gain becomes negative for more increase in signal power > - 10 dBm where in this range of input signal power, the theoretical values of the gain display 0.2 dB at 0 dBm and 4.2 dB at -10 dBm. The difference between the theoretical and experimental results at the two signal powers 0 and 10 dBm is due to the values of loss coefficients and ASE in the theoretical model which are considered.

At 1600 nm, the gain is positive for all values of the input signal power and has a maximum value of 43 dB at - 40 dBm signal power. There is also a fair agreement between experimental and theoretical results, except at 0 dBm signal power, the theoretical gain exceed 8 dB than the experimental gain value due to the loss and ASE effects that are considered in the theoretical model.

The theoretical model is limited to positive values of gain and so there is a difference between theoretical and experimental at the values of input signal power from -10 dBm to 10 dBm

Fig. 4 shows the noise figure of EYCDRHA as a function of input signal power at the same conditions of Fig. 3. The noise figure has minimum values of (~ 3.4dB at 1530 nm) and (5 dB at 1600 nm) for input signal of - 40 dBm. The large values of noise figure are found at input

signal power  $> 0$  dBm at 1530 nm. Furthermore, the noise figure is nearly constant for all values of input signal power at 1600 nm. There is a fair agreement between theoretical and experimental values of the noise figure at 1530 nm till -10 dBm signal power and a slight difference of the theoretical and experimental values of the noise figure at all range of input signal power at 1600 nm.

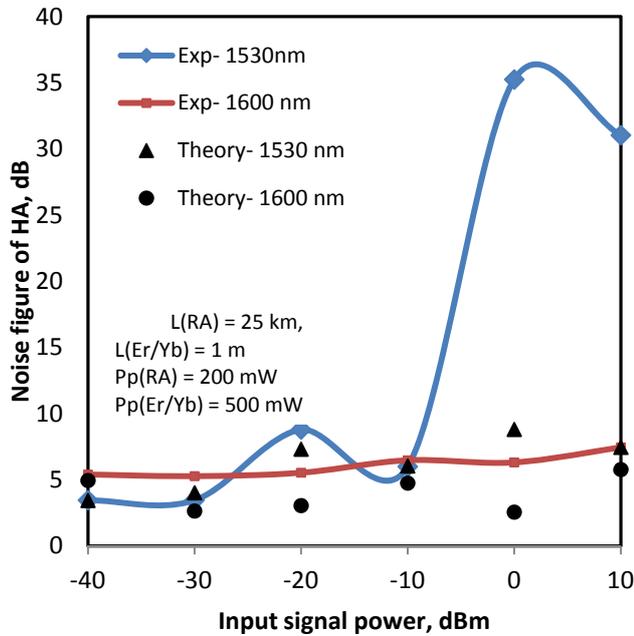


Fig. 4. Noise figure of HA versus the input signal power.

The dependence of the gain and noise figure of EYCDRHA on Er/Yb co-doped 980 nm forward pump power at -40 dBm signal power and RA 1450 nm backward pump power at 200 mW is displayed, respectively, in Figs. 5 and 6. The Er/Yb co-doped fiber amplifier length is RA length is 25 km.

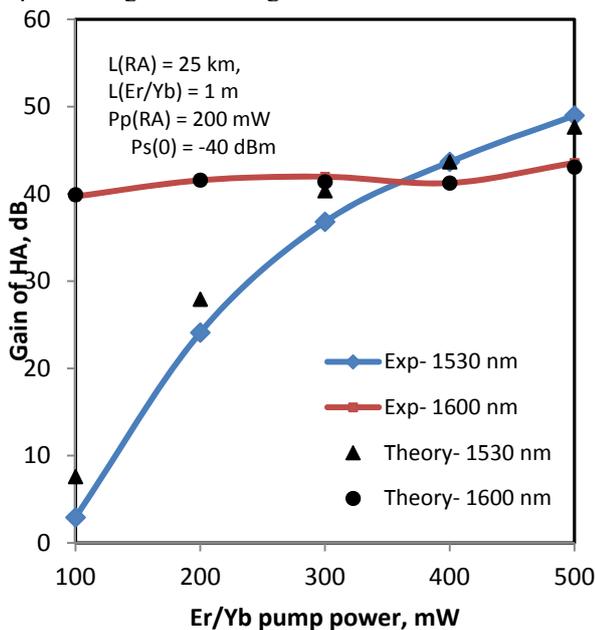


Fig. 5. Gain of HA versus Er/Yb pump power.

In Fig. 5, the gain is nearly constant at 1600 nm. This is because the gain at this range of wavelength is affected largely by the RA pump power and length, which are fixed in this case. At 1530 nm, gain increases with Er/Yb co-doped pump power. There is also a good agreement between theoretical and experimental results.

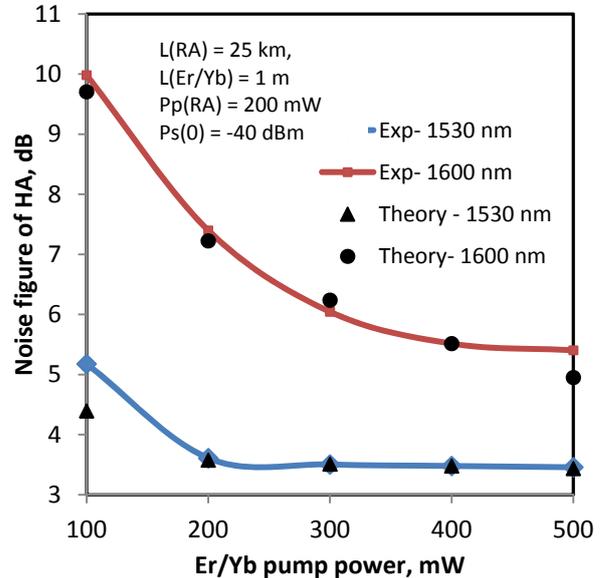


Fig. 6. Noise figure of HA versus Er/Yb pump power.

In Fig. 6, the noise figure decreases with Er/Yb co-doped amplifier pump power and is then saturated at pump power  $> 200$  mW at 1530 nm, while it decreases all over the Er/Yb co-doped pump power range at 1600 nm. The minimum value of noise figure (3.43 dB) is obtained at 500 mW at 1530 nm. Again, there is a good agreement between theoretical and experimental values of noise figure.

The effect of RA pump power on the gain and noise figure of EYCDRHA is displayed, respectively, in Figs. 7 and 8. RA pump power has the range 50-250 mW, at input signal power of -40 dBm, Er/Yb amplifier and RA lengths are 1 m and 25 km, respectively, and Er/Yb pump power is 500 mW.

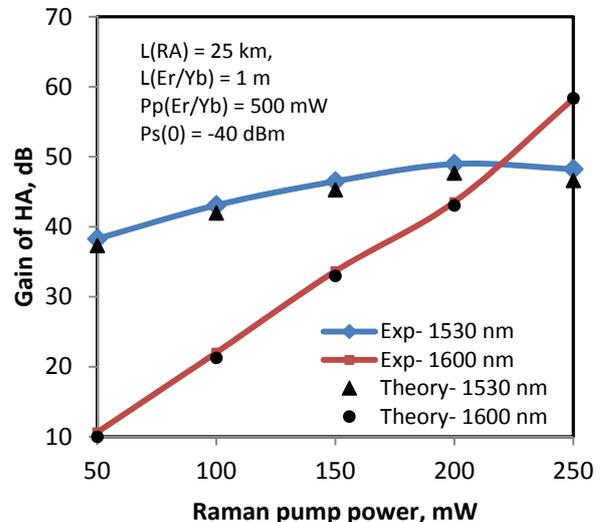


Fig. 7. Gain of HA versus RA pump power.

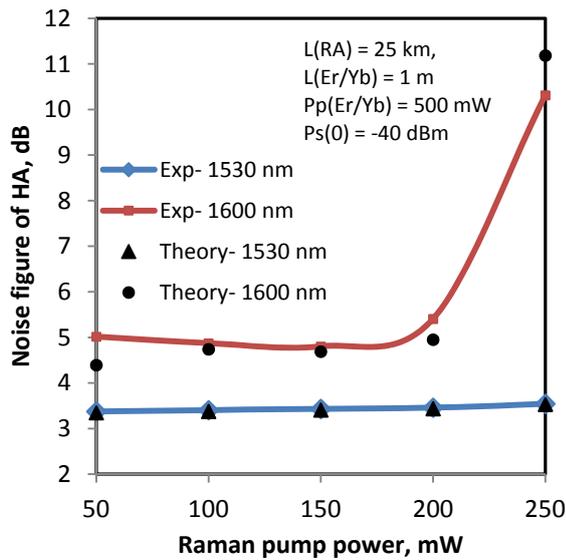


Fig. 8. Noise figure of HA versus RA power.

At 1530 nm signal wavelength, the gain increases with the RA pump power in the range  $< 200$  mW as in Fig. 7. Then, it has a maximum value of  $\sim 49$  dB at 200 mW, for pump  $> 200$  mW, and then begins decreasing. There is a slight difference between experimental and theoretical results of the gain, at this wavelength. Noise figure is nearly constant at this signal wavelength as in Fig.8, and there is good agreement between experimental and theoretical results.

At 1600 nm, the gain is continuously increasing with RA pump power and the noise figure is saturated till 200 mW, then it increases with RA pump power  $> 200$  mW as in Figs. 7 and 8, respectively. Furthermore, there is good agreement between experimental and theoretical results.

Figs. 9 and 10 display, respectively, gain and noise figure of EYCDRHA as a function of Er/Yb co-doped amplifier length.

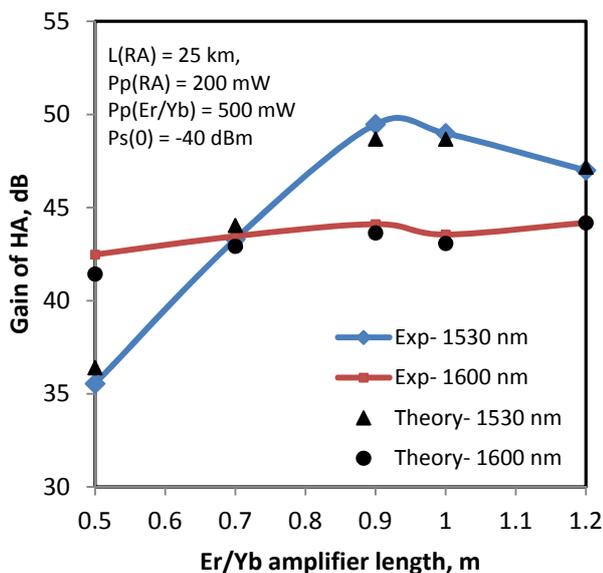


Fig. 9. Gain of HA versus Er/Yb amplifier length.

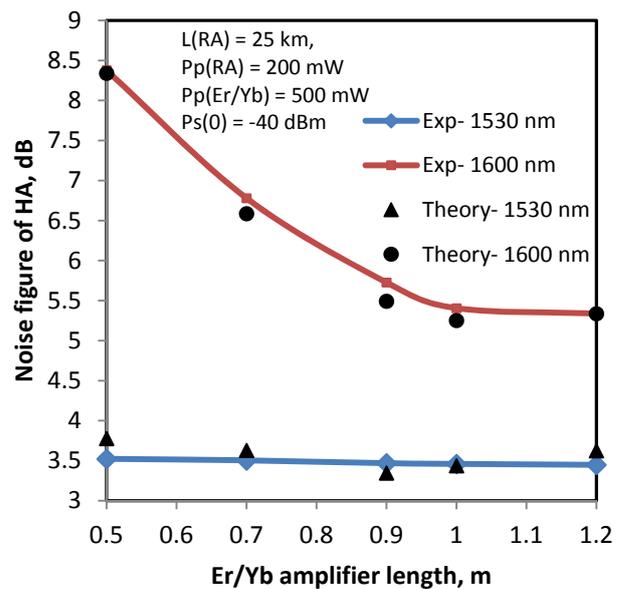


Fig. 10. Noise figure of HA versus Er/Yb amplifier length.

The input signal power is taken - 40 dBm with 25 km of RA length, and Er/Yb and RA pump power of 500 mW and 200 mW, respectively, for the selected signal wavelengths 1530 and 1600 nm.

As seen in Fig.9, both experimental and theoretical models have a maximum gain of  $\sim 49$  dB between 0.9 and 1m of Er/Yb co-doped amplifier length, at 1530 nm with a slight change from 42 to 44 dB in the Er/Yb co-doped amplifier length range at 1600 nm. Furthermore, the experimental noise figure of Fig.10 shows a slightly decrease behavior in the amplifier length range from 3.5 to 3.4 dB at 1530 nm and a strong decrease from 8.3 dB, 0.5 m to 5.2 dB, 1 m, then saturation at Er/Yb co-doped amplifier length  $> 1$  m at 1600 nm. The theoretical noise figure in Fig. 10 is slightly different from experimental values at both signal wavelengths 1350 and 1600 nm due to the same causes discussed in Fig. 3.

The gain and noise figure dependence of EYCDRHA on RA length (10-45 km) are displayed in Figs. 11 and 12, respectively. The input signal power is taken - 40 dBm, Er/Yb amplifier length and pump power are, respectively, 1 m and 500 mW, RA and pump power is kept at 200 mW, for the two selected signal wavelengths 1530 and 1600 nm. At 1530 nm, the EYCDRHA gain increases with RA length till 25 km (with a maximum value of  $\sim 49$  dB) and then decreases. At 1600 nm, the gain continuously increases with RA length.

Fig. 11 shows a good agreement between theoretical and experimental values of the amplifier gain. Noise figure of EYCDRHA, Fig. 12, shows a constant behavior around 3.4 dB as RA length increases at 1530 nm and an increasing behavior with RA length at 1600 nm. The theoretical and experimental results are nearly similar.

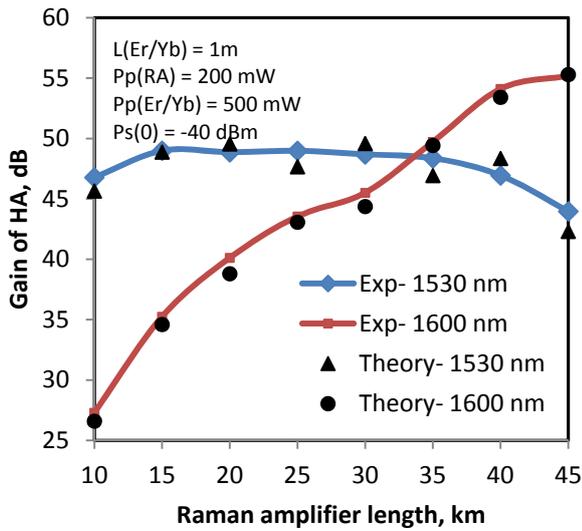


Fig. 11. Gain of HA versus RA length.

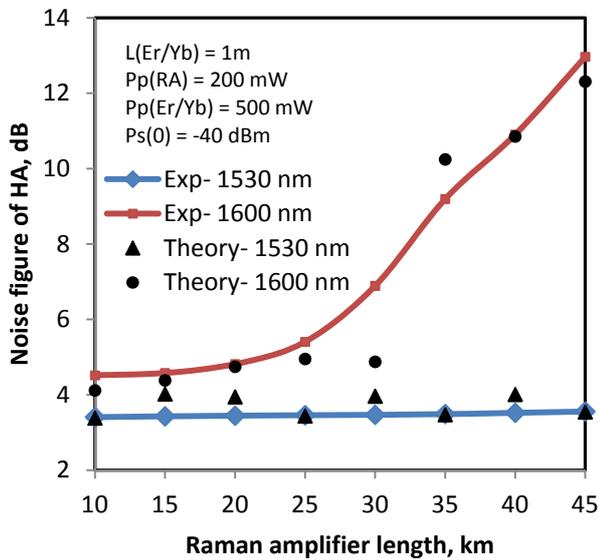


Fig. 12. Noise figure of HA versus RA length.

## 6. Conclusion

In this paper, we experimentally and theoretically studied a hybrid optical amplifier (HA) comprising an erbium ytterbium co-doped fiber amplifier and a Raman amplifier. The EYCDFA is used as pre-amplifier and the RA as a poster one. The effect of the amplifier parameters like length, pump power, signal power and signal wavelength on the HA performance is investigated. The ASE, background losses and the up-conversion of EYCDFA effects are taken into account in the theoretical model. A high gain of 49 dB at 1530 nm and 43 dB at 1600 nm and low noise figure of 3.4 dB at 1530 nm and 5 dB at 1600 nm are obtained. These values are yielded at input signal of -40 dBm with EYDFA and RA pump power of 500 mW and 200 mW, EYDFA and RA lengths of 1 m and 25 km, respectively. Furthermore, a fair agreement is obtained between the experimental and theoretical values of the gain and noise figure.

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