# **Spectroscopic and quantum chemical investigation of the boro-bismuthate glass structure**

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The structural properties of the  $4Bi<sub>2</sub>O<sub>3</sub>·B<sub>2</sub>O<sub>3</sub>$  glass were investigated by FT-IR spectroscopy and quantum chemical calculations. The main results reveal that the coordination polyhedrons of the bismuth ion from the [BiO<sub>6</sub>] structural units and of the boron ion from the  $[BO_4]$  groups are irregular. Accordingly, the  $[BO_6]$  and  $[BO_4]$  structural units in the studied glass matrix have a complex structural role that makes possible the formation of the vitreous system. The structure in the vicinity of the Fermi level shows a metallic behavior.

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# **1. Introduction**

Glasses formed with heavy metal ions have received significant attention because of their interesting optical applications [1, 2].

Quantum chemistry uses a variety of approaches to approximate the solution of the Schrodinger equation for the system of interest. High level structural modeling methods, both ab initio and DFT, take into account all the electrons in the system. Semiempirical methods use some parameters derived from experimental works and deal only with valence electrons. In all cases, optimized structures are calculated by varying the geometrical parameters until an energy minimum is found.

Semiempirical calculations of the pentaborate clusters that are the basic structural units of the alkali-borate glasses were described in previous papers [3, 4]. Other quantum chemical studies deal with the structure of some silica glasses [5].

The main objectives of the present work were to study the structural properties of the boro-bismuthate glasses based on experimental measurements and theoretical models.

## **2. Experimental**

The  $4Bi<sub>2</sub>O<sub>3</sub>$   $B<sub>2</sub>O<sub>3</sub>$  glass system was obtained from homogenized mixtures of  $Bi_2O_3$  and  $H_3BO_3$  reagents of p.a. purity grade by melting at  $1200^{\circ}$ C for 20 minutes in corundum crucibles in an electric furnace. The melts were quenched to room temperature.

The structure of the glasses was investigated by infrared spectroscopy using the KBr pellet technique. The IR spectra were recorded in the  $400-1600$  cm<sup>-1</sup>range using a JASCO FTIR 6100 spectrometer.

The starting structures have been built up using the graphical interface of Spartan'04 [6] and preoptimized by molecular mechanics. Optimizations were continued at ab initio (HF/LanL2DZ/ECP) and DFT (B3BW91/CEP-4G/ECP) level using the Gaussian'98

package of programs [7]. For bismuth atoms the effective core potential (ECP) proposed by Hay and Wadt [8] has been adopted together with the associated basic set. The same ECP has been tested in the framework of DFT by carrying out B3PW91 calculations.

It should be noticed that only the broken bonds at the model boundary were terminated by hydrogen atoms. The positions of boundary atoms were frozen during a calculation and the coordinates of internal atoms were optimized in order to model the active fragment flexibility and its incorporation into the bulk.

 Frequency analysis followed all optimizations in order to establish the nature of the stationary points found, so that all the structures reported in this study are genuine minima on the potential energy surface at this level of theory, without any imaginary frequencies. Accordingly, frequency calculations were performed to ensure that the stationary points were minima and to calculate infrared (IR) spectra. Calculated IR frequencies and intensities were transformed via the SWizard program [9] into simulated IR spectra using Lorentzian functions with half-widths of 15  $cm^{-1}$ .

The fully optimized models obtained by performing ab initio calculations were used to compute the density of state (DOS) and crystal orbital overlap population (COOP) using the BICON-CEDIT package [10].

#### **3. Results and discussion**

The FT-IR spectra of crystalline  $H_3BO_3$  and  $Bi_2O_3$ samples are reported in figure 1a and b. As expected, the widths of the absorption bands of these samples are smaller and the peaks intensities are higher than those of the glass samples. In the spectra of the  $H_3BO_3$  crystal, the strong absorption bands are located at  $\sim$  546, 647, 800 and 1194 cm-1. These infrared absorption bands can be assigned to the B-O-B bending vibrations  $(647 \text{cm}^{-1})$ , the BO<sub>3</sub> triangular unit vibrations  $({}_{8}^{8}00 \text{ cm}^{-1})$  and to the B-O bonds from isolated pyroborate groups  $(1194 \text{cm}^{-1})$ [11]. Some authors [12] suggested that the simultaneous occurrence of the

bands around 930, 770, 650 and 550  $cm<sup>-1</sup>$  is indicative of the presence of pentaborate structural groups.



*Fig. 1. Experimental FT-IR spectrum of the H<sub>3</sub>BO<sub>3</sub> (a) and*  $Bi_2O_3$  (b) reference crystals, of the  $4Bi_2O_3·B_2O_3$  glass *(deconvolution using Lorentzian functions) (c) and of the simulated IR spectrum using Lorentzian functions (calculations DFT) of the model (d).* 

The infrared spectrum of the crystalline  $Bi<sub>2</sub>O<sub>3</sub>$  in the small wave number region,  $400-880$  cm<sup>-1</sup>, presents distinguished IR bands and shoulders located at 435, 507 and  $542 \text{ cm}^{-1}$  that can be attributed to the Bi-O-Bi vibrations [13].

An evidence for the existence of the  $[BiO_3]$  polyhedra is the appearance of a band located around 840 cm<sup>-1</sup> in our spectra [14, 15].

The following bands are present in the spectra of the glasses shown in figure 1c:  $\sim$ 496, 711, 877, 1222 cm<sup>-1</sup>. The infrared band that appears at  $860 \text{ cm}^{-1}$  is attributed to the  $[BO<sub>3</sub>]$  triangular unit vibrations  $[11]$ . The band from 1220  $cm<sup>-1</sup>$  was assigned to the stretching of the terminal B-O bonds of the pyroborate groups [16]. The  $[BO_4]$  vibrations are observable between 900 and 1100 cm<sup>-1</sup> [17].

As we mentioned for the  $4Bi<sub>2</sub>O<sub>3</sub>·B<sub>2</sub>O<sub>3</sub>$  glass, the  $Bi<sup>+3</sup>$ cations are usually incorporated in the glass network as deformed  $[BiO<sub>6</sub>]$  octahedral and  $[BiO<sub>3</sub>]$  pyramidal units. The appearance of a breathing vibration of rings containing  $[BO<sub>3</sub>]$  triangles and  $[BO<sub>4</sub>]$  tetrahedral structural units as a very small band around 785cm<sup>-1</sup> confirms our assumption that the boron atoms from the glass are three and four coordinated [18].

These data were used in the present research in order to compute a possible structural model of the  $4Bi<sub>2</sub>O<sub>3</sub>B<sub>2</sub>O<sub>3</sub>$ boro-bismuthate glass. In general, good similarities were found between the theoretically calculated Bi-O  $(2.02-2.11\text{\AA})$  and B-O  $(1.47-1.51\text{\AA})$  bond lengths from the proposed mechanical-quantum models and the experimental values (figure 2). Instead of this, several distances are slowly diversified. Thus, in figure 2a (I theoretic model) a larger distance was found for the Bi-O bond length  $(3.19\text{\AA})$  from [BiO<sub>6</sub>] unit. This fact was previously reported for the bismuth borate compounds with irregular coordination polyhedra [19,20]. The II investigated model (figure 2b) shows diverse B-O bond lengths (1.52; 1.58; 1.65 and 1.68 Å) from the [BO<sub>4</sub>] units suggesting that the  $[BO_4]$  structural groups are distorted.



 *Fig. 2. The optimized structures of two possible models for the*  $4Bi_2O_3·B_2O_3$  *boro-bismuthate glass used to perform the ab initio (HF/LanL2DZ/ECP) and DFT (B3BW91/CEP-4G/ECP) computations.* 

The Bi-O bond dis tance (3.19Å) is longer than the Bi-O covalent bond (2.22Å) but significantly shorter than

the sum of the Van der Waals radii (3.52Å) implying a cation-anion electrostatic interaction with this one. In the II model the long B-O distances are longer than the covalent B-O bond distances (1.51Å) but shorter than the sum of the Van der Waals radii (3.52Å). This leads to a much more unsymmetrical coordination of the II model in the vicinity of  $[BO_4]$  structural units.

The most stable model is the first one (E=-42.7145au/atom) because the total energy/atom is bigger in absolute value than that of the second model (E=-8.3218au/atom). The coordination polyhedra of the bismuth ion from the  $[BiO_6]$  structural units and of the boron ion from [BO4] structural groups are irregular and the thermodynamic stability of the model increases when the octahedra of the  $[BIO_6]$  structural units are more distorted.

We mention that the two studied models describing the local disorder in  $4Bi<sub>2</sub>O<sub>3</sub>B<sub>2</sub>O<sub>3</sub>$  glasses are highly possible but are not unique. However, by using other methods than the HF(LanL2DZ/ECP) or DFT (B3BW91/CEP-4G/ECP) utilized in the present paper, the results concerning the Bi-O and B-O bonds length will not change significantly.

Accordingly, these structural models show a very complex behavior and their stabilization can be achieved by several metallic cations [21] or the adequate arranging of these cations into the vitreous network.

The frequencies and relative intensities of the stretching and bending vibrations of the structural groups from the studied models are presented in figure 1d. The calculated absorption spectrum of the proposed model is in good agreement with the experimental absorption data.

In order to understand the electronic nature of this material, we have explored the density of states designed for the atomic valence orbitals of bismuth, oxygen and boron. In figure 3a and 4 are plotted total, partial DOS and IDOS diagrams indicating that the system have a metallic behavior in the vicinity of the Fermi level. The dashed horizontal line represents the Fermi level,  $E_F$  at -11.2301eV.



*Fig. 3. a) The Total Density of States plots of*  $4Bi_2O_3B_2O_3$ *glass in the energy region from -28eV and 10eV. The dotted horizontal line indicates the Fermi level; b) ICOOP(E), COOP(E) curves for all relevant atom-atom interactions in the*  $4Bi_2O_3B_2O_3$  *glass.* 

The region under the Fermi level has contributions from the O (2s, 2p) derived states and an admixture of the Bi (6s, 6p) and B (2s, 2p) orbitals. The conduction bands consist of a mixture of the B(2s, 2p), Bi(6s, 6p) and O(2p) derived states.

The oxygen projection shows a sharp peak below the Fermi level, at about -26.23eV. This peak can be ascribed to the O(2s) orbitals. Note that the location of this peak is relatively far away from the Fermi level (at about 15eV below the Fermi level). We mention that such low values of the O(2s) states were previously reported for some silicate glasses (with the O(2s) peak located at about -16.5eV) [22-24]. This location may be due to the contribution of the nonbridging oxygen atoms present in the glass network [22-24].



*Fig. 4. The partial DOS(E) diagrams of the clusters from the*  $4Bi_2O_3$ *·B<sub>2</sub>O<sub>3</sub></sub> glass.* 

The Fermi level is located in the middle of the Van Hove singularities corresponding to the B s-orbital and Bi-s orbital derived states. This is considered an indication that there is an overlap with oxygen orbitals. The Van Hove singularities corresponding to bismuth and boron orbital derived states are cleft suggesting that there are strong boron-oxygen and bismuth-oxygen interactions. This agrees with the results of the ab initio calculations that show the presence of Bi-O and B-O bonds with variable lengths.

We have applied the COOP scheme [25] to analyze the chemical bonds into the two clusters elaborated in order to model the structure of the  $4Bi<sub>2</sub>O<sub>3</sub>·B<sub>2</sub>O<sub>3</sub>$  glass (figure 3b). COOP describes the density of bonding and antibonding interaction between specific orbitals at a given energy in solids. Regions with positive COOP contributions are bonding, those with negative COOP contributions are antibonding and the ones with zero COOP contributions are nonbonding [26]. In order to determine the overall interaction of two atoms at a given distance, bonding and antibonding contributions are integrated up to the Fermi level.

The integration of the COOP (ICOOP) curve is maximal below, above and just at the Fermi level for B-O bonds. The electron filling is optimal for boron- oxygen interaction indicating strong B-O bonding [25].

The valence band consists of the  $O(2p)$ ,  $B(2s, 2p)$  and Bi (6s, 6p) hybrids, forming bonding and antibonding states separated by nonbonding bands. The bonding B-O interaction is only slightly weakened by an antibonding region just below the valence band edge while the bonding Bi-O interaction is located on the top of the conduction band and was found to be very important for the stability of the calculated structural model.

#### **4. Conclusions**

The combined FT-IR spectroscopy data and quantum chemical calculations of the  $4Bi<sub>2</sub>O<sub>3</sub>·B<sub>2</sub>O<sub>3</sub>$  glass system evidence that the  $Bi^{+3}$  cations are incorporated in the glass network as  $[BiO<sub>3</sub>]$  pyramidal,  $[BiO<sub>6</sub>]$  octahedral and as distorted  $[BiO_6]$  octahedral units. On the other hand a strong distortering effect of  $Bi<sub>2</sub>O<sub>3</sub>$  on the vitreous  $B<sub>2</sub>O<sub>3</sub>$ network is demonstrated and this effect increases when the boron cation of the  $[BO_4]$  unit is situated in the vicinity of a boroxol ring.

The Van Hove singularities corresponding to bismuth and boron orbital derived states are cleft suggesting that there are strong boron-oxygen and bismuth-oxygen interactions. This explains the results obtained by the ab initio calculations that show diverse Bi-O and B-O bond lengths. The  $[BiO_6]$  and  $[BO_4]$  structural units that build up the studied glass network have a complex structural role that makes possible the formation of the  $4Bi<sub>2</sub>O<sub>3</sub>·B<sub>2</sub>O<sub>3</sub>$ vitreous system.

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