

# Turn-on time delay characteristics of external cavity laser based polymer fiber gratings

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The turn-on time delay ( $T_{Delay}$ ) characteristics of an external cavity laser-based polymer fiber gratings (PFGs) is successfully investigated. Numerical optimization of model parameters is used to reduce the laser  $T_{Delay}$  by analyzing the effects of the laser injection current ( $I_{inj}$ ), the temperature ( $T$ ) variation, the recombination rate  $R(N)$  coefficients, and the external OFB level on  $T_{Delay}$ . Results show that the effect of  $R(N)$  coefficients are to increase the  $T_{Delay}$  value and not decrease it as written in the previous studies. Also, results show that the  $T_{Delay}$  value is increased when  $T$  is increased. However, we can eliminate it either by increasing the  $\rho$  value (i.e.  $\rho = N_i/N_{th}$ ) at a fixed value of  $I_{inj}$  or by increasing the  $\sigma$  value (i.e.  $I_{inj} = \sigma \times I_{th}$ ) at constant  $I_{th}$ . In addition, we can use the external optical feedback (EOF) level as a controller for reducing the  $T_{Delay}$  value or to turn-on the laser by controlling the  $N_{th}$  value depending on the EOF level.

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## 1. Introduction

The last two decades of the last century, due to the growing demand for massive data transmission, showed a noticeable increase in the use of optical fiber gratings (FGs) as an indispensable tool in many important applications [1-4], where the external environment such as stress [5, 6] and temperature [7-9] plays a dominant role due to its unique characteristics such as wavelength selection [10-12] and low loss [13-15]. However, for silica fiber gratings (SFGs), limited tunability is a major drawback of this important tool [3, 4] which reduces its reliability in many important applications [13-15].

In the case of polymer fiber gratings (PFGs) the situation is totally different; the thermal and strain characteristics are much higher than that of the SFGs [16]. For example, the Young's modulus for the polymer is 70 times smaller than that of silica (i.e.  $0.1 \times 10^{10}$  N/m<sup>2</sup> compare with  $7.13 \times 10^{10}$  N/m<sup>2</sup>), which make the mechanical tunability is much better than that of SFGs. In addition, PFGs has the merits of a large thermo-optic effect, thereby, large refractive index tuning can be obtained. Furthermore, the flexibility of the PFGs can make the tunability extend beyond the thermo-optic effect limit [17]. Based on the mention facts, PFGs has better potential to be used as wavelength tuning and sensing element.

The widespread use of systems based on wavelength division multiplexing (WDM) networks [18-20], which are characterized by their complete reliance on a highly stable laser source with a large possibility of tuning, make fiber gratings (FGs) based on external cavity lasers (ECLs) an

indispensable source [21-24]. The reason for this is that the ECL emission wavelength depends only on the Bragg wavelength of the FGs and does not depend on the injection current ( $I_{inj}$ ) of the laser cavity [25-27]. Therefore, ECLs are a promising source of light for receiver-dense WDM (DWDM) systems. Furthermore, the wavelength of FGs can be controlled more precisely than other laser models. As a result, ECLs achieve much better wavelength control [28, 29].

Generally, in laser diodes (LDs), a parameter known as a turn on time delay ( $T_{Delay}$ ) is very important. It is defined as the time required for populating the carriers ( $N$ ) to reach its threshold level ( $N_{th}$ ) where the initial level of current ( $I_o$ ) changes to any current value ( $I$ ) larger than its laser threshold current ( $I_{th}$ ). This happens when LDs are injected by an injection current ( $I_{inj}$ ) [30]. During this period, the concentration of photons ( $P$ ) suffers a relaxation oscillation until it reaches its steady state value [31]. For longer  $T_{Delay}$  value, the relaxation oscillation period is also longer, which may result a significant error in received-data when the laser is used in high-speed transmission systems [30-31].

The  $T_{Delay}$  is one of the most important parameters that play a major role in determining the performance characteristics of the communication systems [31]. It was found that it is strongly dependent on the functional form of the carrier recombination rate  $R(N)$  coefficients [30-32]. However, most of the previous studies relied in their results on approximate relationships or equations in which one or more of the influential parameters were neglected [30, 33]. In addition to the inaccuracy in the results, these assumptions cancel out the influence of some important

parameters in determining the true dynamic behavior of the system. On the other hand, to our knowledge there is no study that dealt with this important parameter of ECLs based on PFGs, as all previous studies were concerned with SFGs.

The continuous increase in the versatility of promising applications within the optical communication systems and optical sensing fields makes PFGs an indispensable tool in the coming days, so studying the dynamic properties of PFGs based on ECLs is essential.

## 2. Laser model

A schematic diagram of the ECL model is shown in Fig. 1. In this model, ECL consists of Fabry-Perot (FP) laser diode with length  $L_d$ . The front facet reflectivity is approximately zero ( $R_1 \approx 0$ ), while the rear facet has a finite reflectivity  $R_0$  that is coupled to a single-mode fiber (SMF) of length  $L_f$  with coupling coefficient  $C_o$ . The PFGs with reflectivity  $r_{FBG}$  is connected at the end of SMF.

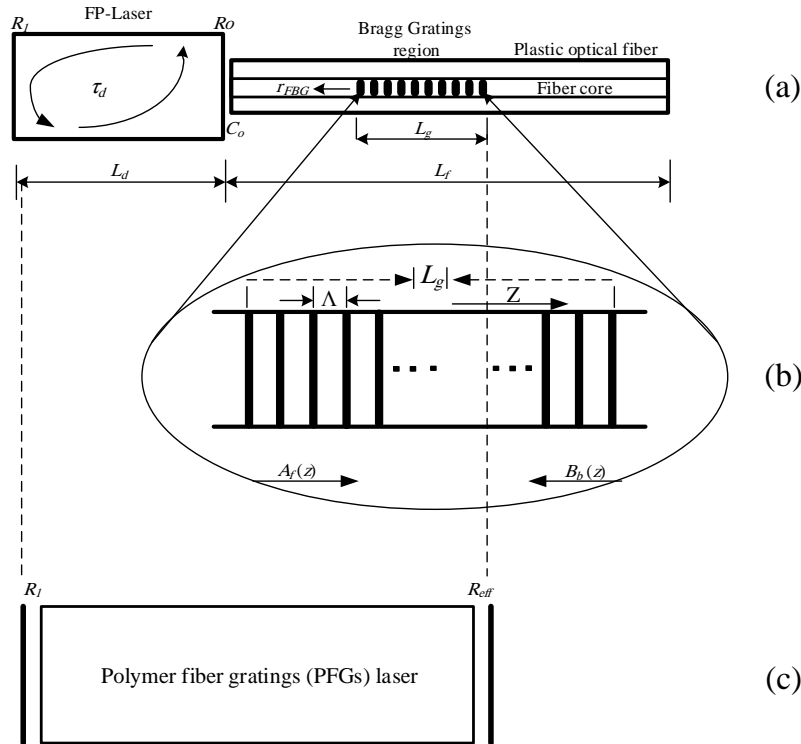


Fig. 1. ECL model based PFGs

Based on Fig. 1 (c), the effective reflectivity  $R_{eff}$  is given by [32]

$$R_{eff} = |r_{eff}|^2 = |R_0(1 + F_{ext} \times \cos(2\pi\nu\tau_e))|^2 \quad (1)$$

where  $\nu$  is the optical frequency,  $\tau_e = 2n_{ext}L_f/c$  is the round-trip delay of photons inside the external cavity,  $c = 3 \times 10^{10}$  cm/s is the velocity of light in vacuum,  $n_{ext}$  is the external cavity refraction index and  $F_{ext}$  is a factor is due to the external cavity given by [32]

$$F_{ext} = \frac{r_{ext}}{R_0} (1 - |R_0|^2) \quad (2)$$

where  $r_{ext}$  is the external optical feedback (EOF) reflection coefficient of the PFGs.

By considering the combine effect of the temperature (T) and external optical feedback (EOF), the threshold current [9] is given as

$$I_{th, EOF}(T) = eVN_{th, EOF}(T)R(T, N_{th, EOF}) \quad (3)$$

In Eq. (3),  $e$  is the electronic charge,  $V$  is the active region volume and  $R(T, N_{th, EOF})$  is the carriers recombination rate [31] can be rewritten as

$$R(T, N_{th, EOF}) = A_{nr} + BN_{th, EOF}(T) + CN_{th, EOF}^2(T) \quad (4)$$

where,  $A_{nr}$  is the nonradiative recombination rate,  $B$  is the radiative recombination rate and  $C$  is the Auger recombination rate, respectively. In Eq. (4), the

$N_{th, EOF}(T)$  represent the threshold carrier density [31], can be defined as

$$N_{th, EOF}(T) = N_t(T) + \frac{1}{\Gamma v_g g(T) \tau_{p, EOF}(T)} \quad (5)$$

In Eq. (5),  $N_t(T)$  represent the carrier density at transparency,  $g(T)$  is the gain coefficient, and  $\tau_{p, EOF}(T)$  is the photon life time which can be modeled as [31]

$$\tau_{p, EOF}(T) = \frac{1}{v_g \alpha_{tot, EOF}(T)} \quad (6)$$

where  $\alpha_{tot, EOF}(T)$  is the total cavity loss that is defined as [31]

$$\alpha_{tot, EOF}(T) = \alpha_{int}(T) + \frac{1}{2L_d} \ln \left( \frac{1}{R_1 R_{eff}} \right) \quad (7)$$

In Eq. (7),  $\alpha_{int}(T)$  and  $\left( \frac{1}{2L_d} \ln \left( \frac{1}{R_1 R_{eff}} \right) \right)$  represents the internal cavity and the mirror losses, respectively. According to the Eqs. (1) – (7), the  $N_{th, EOF}(T)$  can be expressed as

$$N_{th, EOF}(T) = N_t(T) + \Theta(T) \quad (8)$$

where,

$$\Theta(T) = \frac{\left( \alpha_{int}(T) + \frac{1}{2L_d} \ln \frac{1}{R_1 |R_2(1 + F_{ext} \times \cos(2\pi\nu\tau_e))|^2} \right)}{\Gamma g(T)} \quad (9)$$

Equation (8) represent the expression for the carrier density under the threshold condition of the ECL model.

### 3. The $T_{Delay}$ formula of ECL model based PFGs

As we have defined in the introduction part, the  $T_{Delay}$  represent the time is needed by the carrier density ( $N$ ) to increases from a specified initial value ( $N_i$ ) to the threshold one ( $N_{th}$ ). This time (i.e.  $T_{Delay}$ ) can be calculated by [31]

$$T_{Delay} = \int_{N_i}^{N_{th, EOF}} \frac{eV}{I_{inj} - eVN(A_{nr} + BN + CN^2)} dN \quad (10)$$

After considering the effect of the  $R_{eff}$  for the PFGs given in Ref. [31], Eq. (10) can be solved numerically to

study the  $T_{Delay}$  characteristics of the ECL model based PFGs. This solution can be written as [31]

$$T_{Delay} = \xi \Pi_1 X_1 + \xi \Pi_2 X_2 + \xi \Pi_3 X_3 \quad (11)$$

where,

$$X_1 = \ln \left[ \frac{\Theta(\Pi_1, N_{th, EOF})}{\Theta(\Pi_1, \rho N_{th, EOF})} \right] \quad (12)$$

$$X_2 = \ln \left[ \frac{\Theta(\Pi_2, N_{th, EOF})}{\Theta(\Pi_2, \rho N_{th, EOF})} \right] \quad (13)$$

$$X_3 = \ln \left[ \frac{\Theta(\Pi_3, N_{th, EOF})}{\Theta(\Pi_3, \rho N_{th, EOF})} \right] \quad (14)$$

$$\Theta(\Pi_m, N) = B + \Xi_1 \Pi_m + \Xi_2 N \quad (15)$$

$$\Xi_1 = (A_{nr} B \xi + 9CI_{inj}) \quad (16)$$

$$\Xi_2 = \left[ (2B^2 - 6A_{nr}C) \xi \Pi_m + 3C \right] \quad (17)$$

$$\Pi_1 = \frac{1}{6\xi} \frac{\Re_2}{\Re_1} + 2 \left( 3A_{nr}C - B^2 \right) \frac{\xi}{\Re_4} \quad (18)$$

$$\Pi_2 = \frac{-1}{2} \Phi_1 + j \frac{\sqrt{3}}{2} \Phi_1 \quad (19)$$

$$\Pi_3 = \frac{-1}{2} \Phi_1 - j \frac{\sqrt{3}}{2} \Phi_1 \quad (20)$$

$$\Phi_1 = \left( \frac{1}{6\xi} \frac{\Re_2}{\Re_1} + 2 \left( 3A_{nr}C - B^2 \right) \frac{\xi}{\Re_4} \right) \quad (21)$$

$$\Re_1 = \xi^2 A_{nr}^2 \Omega_1 + \xi B I_{inj} \Omega_2 + 27C^2 I_{inj}^2 \quad (22)$$

$$\Omega_1 = (4A_{nr}C - B^2) \quad (23)$$

$$\Omega_2 = (18A_{nr}C - 4B^2) \quad (24)$$

$$\Re_2 = \left[ \xi^2 \Re_1 \left( -108C + 12\sqrt{3}\Re_3^{1/2} \right) \right]^{1/3} \quad (25)$$

$$\Re_3 = \frac{\Re_4}{\Re_1} \quad (26)$$

$$\mathfrak{R}_4 = 4\xi^2 B^2 \Omega_3 + 108\xi BC^2 I_{inj} \Omega_4 + 729C^4 I_{inj}^2 \quad (27)$$

$$\Omega_3 = \left( 20.25 A_{nr}^2 C^2 - 9 A_{nr} B^2 C + B^4 \right) \quad (28)$$

$$\Omega_4 = \left( 4.5 A_{nr} C - B^2 \right) \quad (29)$$

Also,  $\xi = eV$  and  $\rho$  ( $0 < \rho < 1$ ) represents the ratio of the  $N_i$  to the (i.e.  $\rho = N_i / N_{th}$ ).

#### 4. Results and discussion

In our numerical analysis, constant value of injection current is assumed;  $I_{inj} = \sigma \times I_{th}$  ( $\sigma$  is an integer value) and it is independent of  $I_{th}$ . For other main parameters, the common values used in the analysis are tabulated in Table 1.

Table 1. Parameters of ECL model based PFGs at room temperature (25°C)

| Parameter                          | Description                            |
|------------------------------------|--|
| $L_d = 400 \mu m$                  | Cavity length                          |
| $d = 0.1 \mu m$                    | Active region thickness                |
| $w = 2 \mu m$                      | Active region width                    |
| $N_o = 1.10^{24} m^{-3}$           | Transparency carrier density           |
| $A_{nr} = 1.10^8 \text{ sec}^{-1}$ | Nonradiative recombination coefficient |
| $B = 1.10^{-16} m^3 / \text{sec}$  | Radiative recombination coefficient    |
| $C = 3.10^{-41} m^6 / \text{sec}$  | Auger recombination coefficient        |
| $\alpha_{int} = 1000 m^{-1}$       | Internal cavity loss                   |
| $\Gamma = 0.34$                    | Field confinement factor               |
| $a_o = 2.5.10^{-20} m^2$           | Differential gain                      |
| $L_{FBG} = 4 mm$                   | Grating length                         |
| $\lambda = 1550 \text{ nm}$        | Operating wavelength                   |

Fig. 2 shows  $T_{Delay}$  for PFGs model as a function to the carrier density ratio (i.e.  $\rho = N_i / N_{th}$ ) for different values of  $\sigma$  at reference temperature ( $T = 25^\circ C$ ).

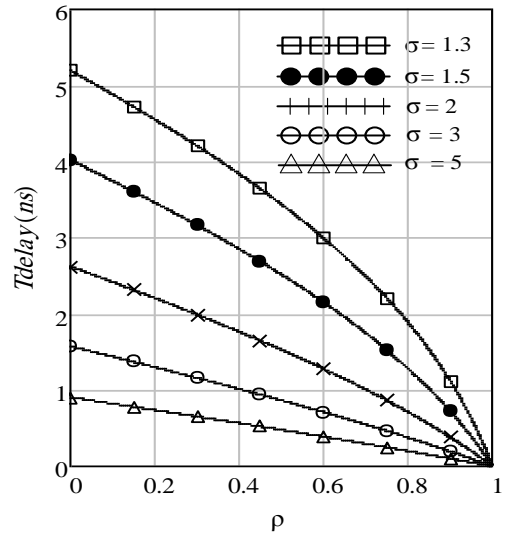


Fig. 2. Turn-on delay time function to  $\rho$  for different values of  $\sigma$

As shown, with the increases of the  $\rho$  value,  $T_{Delay}$  reduces. This result agrees with the assumption that, when  $N_i$  reaches  $N_{th}$ , the  $T_{Delay}$  value will be zero [31]. As a result, when the laser biased near  $N_{th}$ , the  $T_{Delay}$  can be eliminated.

Fig. 3 shows a comparison between the  $T_{Delay}$  calculation by our exact numerical expression model and other approximated equations in the previous studied [30, 31, 33] for  $\sigma = 1.3$ . As shown, there are differences in the  $T_{Delay}$  values. This difference is due to the neglected one or more of the  $R(N)$  coefficients (i.e.  $A_{nr}$ ,  $B$ ,  $C$ ). The validity of our results can be confirmed by the following interpretation: according to Eq. (4), any increment in the  $A_{nr}$ ,  $B$ , and  $C$ ; the  $T_{Delay}$  increases due to the increases of the carrier recombination rate time;  $R(N)$  which results in an increase in the threshold current of the laser (i.e. Eq. (3)).

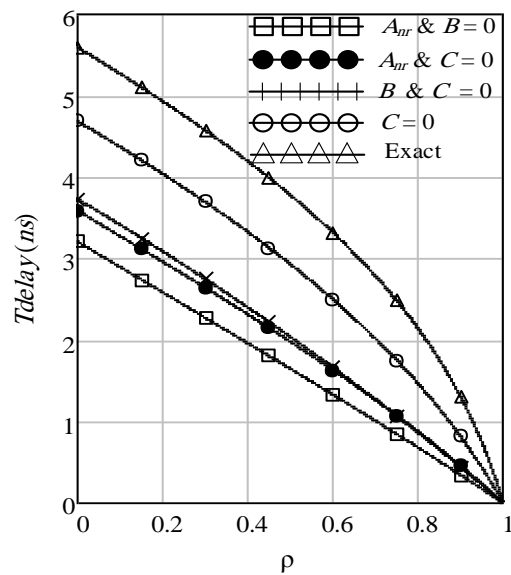


Fig. 3. A comparison among various expressions of turn-on delay time with  $\rho$  at  $\sigma = 1.3$

As it is known, the higher the threshold current ( $I_{th}$ ), the greater  $T_{Delay}$  required to reach the threshold value. This meaning that, the effect of increasing any one of the  $R(N)$  coefficients, is to increase the  $T_{Delay}$  value as shown in Fig. 4. It is important to mention here that this result is completely contrary to that is given in the [33]. Thus,

according to the results given in Fig. 4, the general effect of the  $R(N)$  coefficients are to increases the  $T_{Delay}$  value as they increase. So the  $T_{Delay}$  can be reduce either by reduce  $R(N)$  coefficients at fixed value for  $I_{inj}$  or by increasing  $I_{inj}$  at constant  $I_{th}$ . These results indicate preference model proposed by us compared with previous studies.

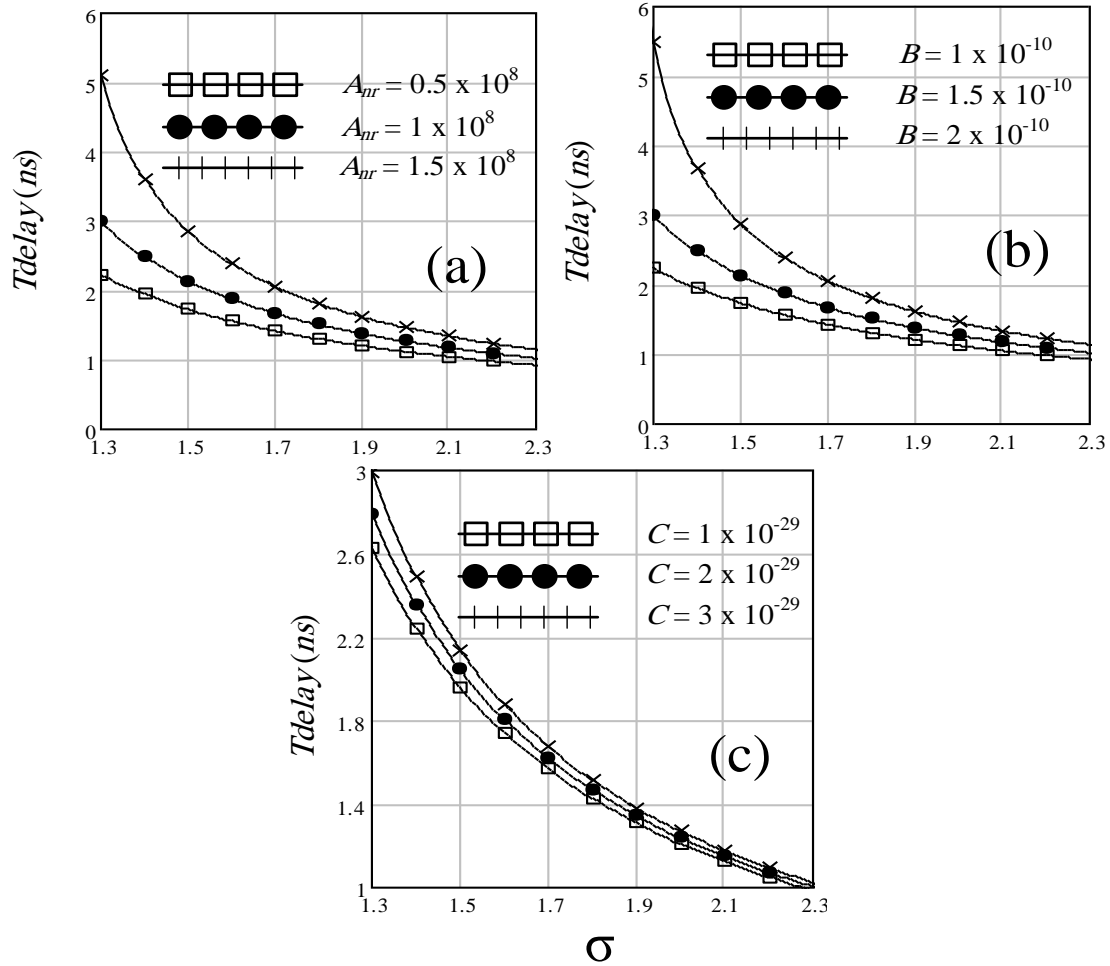


Fig. 4. Effect of  $R(N)$  coefficients on turn-on time delay at  $\rho = 0.5$ . (a)  $A_{nr}$ , (b)  $B$  and (c)  $C$  coefficients, respectively

Fig. 5 (a) and (b) shows the effect of temperature ( $T$ ) on  $T_{Delay}$  for different values of  $\rho$  at  $\sigma = 1.3$  for PFGs and SFGs, respectively. In general, it is clear that the  $T_{Delay}$  is increases with the increase of  $T$  due to its effect on the  $N_{th}$  value (i.e. according to Eq. (8)). However, the effect of temperature can be eliminated by increasing of the  $\rho$  value. This result can explain as, when  $\rho \rightarrow 1$ , i.e.  $N_i \rightarrow N_{th}$ , therefore,  $T_{Delay} \rightarrow 0$ . Thus, when the laser source turned

on from  $N_i$  closed to the  $N_{th}$  value, the  $T_{Delay}$  can be eliminate. Also according to the results shown in Fig. 5, the  $\rho$  value is represented a significant factor for reducing the  $T_{Delay}$  value especially in the direct modulation of LDs where  $N_i$  is varied depending on the time intervals. Thus, if the time interval is relatively short, then, the value of  $\rho$  have the significant effect in reducing  $T_{Delay}$ .

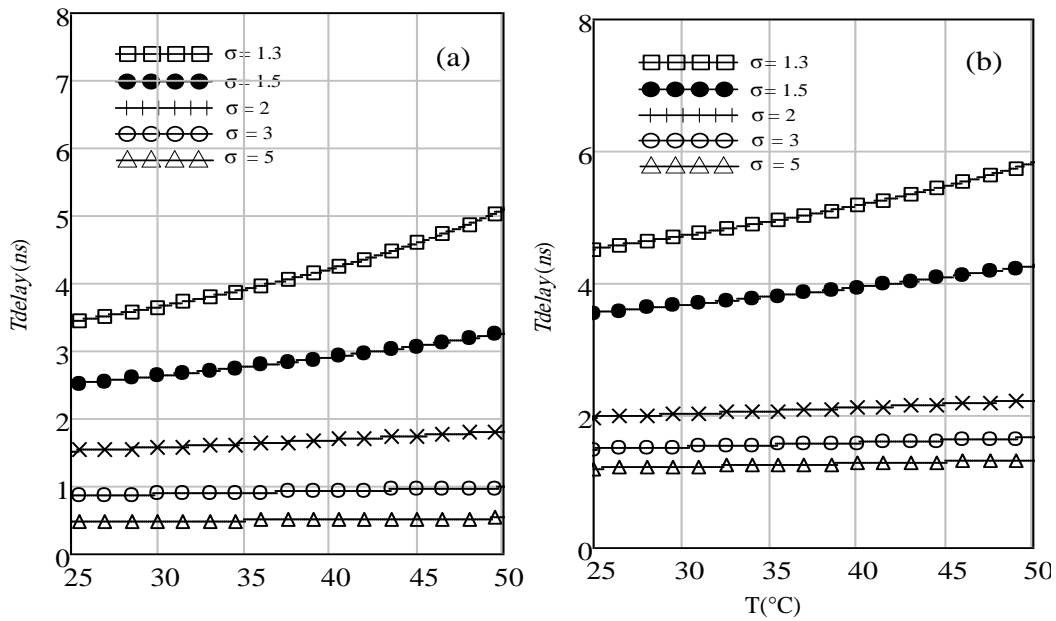


Fig. 5. Effect of temperature on  $T_{Delay}$  for different values of  $\sigma$  at  $\rho = 0.5$ . (a) PFGs and (b) SFGs

On the other hand, by comparing Fig. 5 (a) and (b), it can be seen that there is a difference between the  $T_{Delay}$  value for the two cases. And to be more precise, the  $T_{Delay}$  in the case of the PFGs with the change in temperature is less than it is in the case of SFGs. The reason for this is due to the change of the  $R_{eff}$  value of both cases with temperature as shown in Fig. 6 which in turn greatly affects the  $T_{Delay}$  value based on the Eqs. (1) - (29). Also, the results in Fig. 5 show that with the increase of the  $\sigma$  value, the  $T_{Delay}$  is reduced at specified value of  $\rho$  and the effect of temperature is eliminated. Thus, depending on the results shown in Fig. (5), the effect of temperature on  $T_{Delay}$  can be eliminated either by increasing of the  $\rho$  value at a fixed injection current ( $I_{inj}$ ) or by increasing of the  $\sigma$  value at constant  $I_{th}$ .

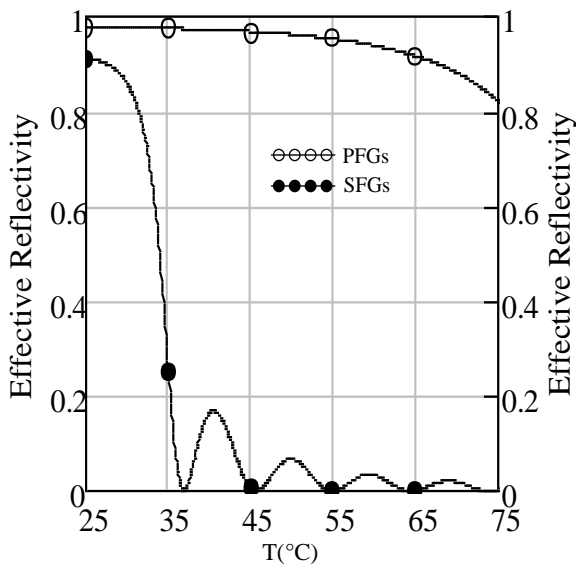


Fig. 6. Effect of temperature on effective reflectivity ( $R_{eff}$ ) for PFGs and SFGs

Finally the effect of external optical feedback (EOF) reflectivity;  $R_{ext}$  on the  $T_{Delay}$  as a function of  $\sigma$  at  $\rho = 0.5$  is shown in Fig. 7. As shown, the  $T_{Delay}$  value is decreases with the increase of the  $R_{ext}$  value. The reason for this can be explained as follows: by increasing the  $R_{ext}$  value, the  $R_{eff}$  will increase (i.e. Eq. (1)) and that results in a reduction in the total cavity loss (i.e. Eq. (7)), and an increasing in the photon life time (i.e. Eq. (6)). Consequently, the  $N_{th}$  value will decrease as given in Eq. (8). This result suggests that EOF can be used as a controller or an optical switching circuit to laser turn-on by controlling the  $N_{th}$  value.

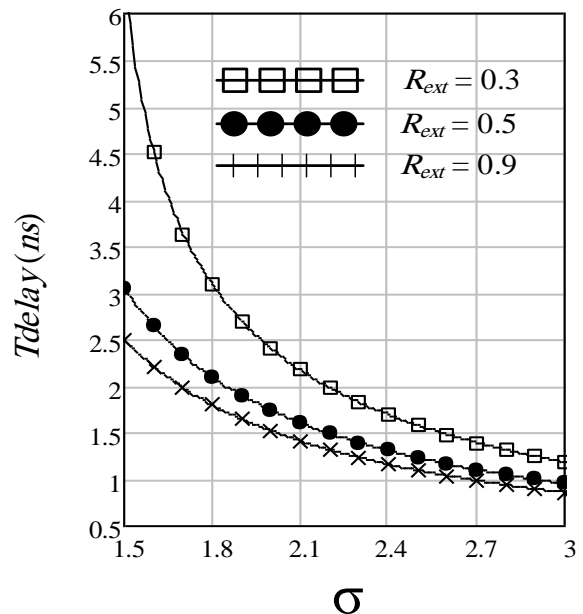


Fig. 7. Effect of  $R_{ext}$  on turn-on time delay at  $\rho = 0.5$

## 5. Conclusion

A numerical study on the turn-on time delay ( $T_{Delay}$ ) characteristics of an external cavity laser (ECL) model-based polymer fiber gratings (PFGs) is successfully investigated. The analysis has done based on an exact numerical formula and not by using approximated formulas as in previous studies. Results show that the effect of the  $R(N)$  coefficients is to increasing the  $T_{Delay}$  value and not as reported in the previous studies. Also, results show that, the effect of temperature is to increase the  $T_{Delay}$  and its effect is less than that of the SFGs. However, temperature effect can be eliminated either by increasing  $\rho$  at a fixed value of injection current ( $I_{inj}$ ) or by increasing  $\sigma$  at constant laser threshold current ( $I_{th}$ ). In addition, we can put down or reducing the  $T_{Delay}$  value by controlling the  $N_{th}$  value through the use of the EOF level.

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